

# SPEED, VELOCITY, ACCELERATION

- Average speed:  $\frac{\text{Total distance}}{\text{total time taken}}$

(Speed: scalar quantity)

velocity may change though the speed remains constant if the direction only changes.

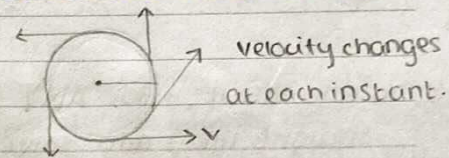
But if speed changes  $v$  changes

- Velocity

- (i) Average velocity: rate of change of displacement.

$$v = \frac{\Delta x}{\Delta t} \quad \frac{\text{total displacement}}{\text{total time}}$$

( $v$ : vector quantity)



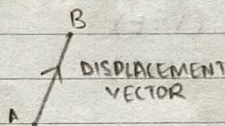
- (ii) Instantaneous velocity: velocity of a body at a given instant of time.

- Displacement: shortest distance between 2 points / directional distance. (vector quantity).

eg. 150 m due north

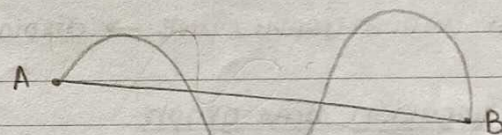
eg. 150 m +ve direction.

The final position / location.



- Distance: length of path travelled by body (scalar quantity)

eg. 150 m



Distance =

Displacement =

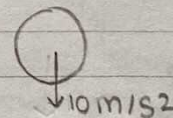
- Acceleration: state of change of velocity.

- (i) Average acceleration =  $\frac{\text{change in velocity}}{\text{time taken}}$

$$a = \frac{\Delta v}{\Delta t}$$

$$a = \frac{\Delta \left( \frac{\Delta x}{\Delta t} \right)}{\Delta t}$$

$$a = \frac{v - u}{t}$$



velocity of the body changes by 10 m/s every second

## FORMULAE

$$v = u + at \quad (\text{as } a = \frac{v-u}{t}) \text{ for constant } a.$$

$$s \text{ or } x = ut + \frac{1}{2}gt^2$$

$$v^2 = u^2 + 2ax$$

↓

$$\text{if } u=0, s = \frac{1}{2}at^2 \text{ and } v = at.$$

$t=0s$   $v = 0 \text{ m/s}$

$t=1s$   $v = 10 \text{ m/s}$

$t=2s$   $v = 20 \text{ m/s}$

$\Delta t = \text{time interval}$



## Vector and scalar

vector quantities: physical quantities with magnitude and a direction.  $\vec{v}$ ,  $\vec{a}$ ,  $\vec{p}$

Scalar: quantities: physical quantities with only magnitude.  
 $m, t$

Distance: summation of all individual displacements btwn 2 points.

speed: magnitude of velocity.

## Acceleration

Positive acceleration:

- (i) acceleration in which the velocity increases
- (ii) acceleration in the velocity's direction

Negative acceleration:

- (i) acceleration in which the velocity decreases.
- (ii) acceleration in the opposite direction to the velocity.



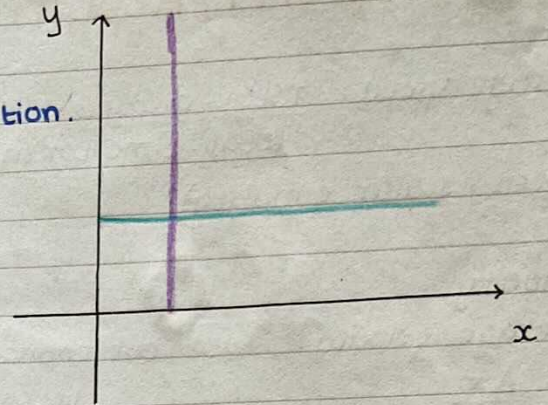
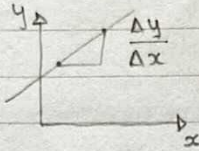
# MOTION GRAPHS (UNIFORM MOTION)

every straight line can be expressed as a linear equation.

$$y = mx + c$$

m = slope and c = y intercept

Slope =  $\frac{\Delta y}{\Delta x}$  OR  $\frac{y_2 - y_1}{x_2 - x_1}$



To calculate it, take ANY 2 points (on a straight line) and solve  $y_2 - y_1 \div x_2 - x_1$ .

y is constant slope = 0  
x is constant slope = ∞



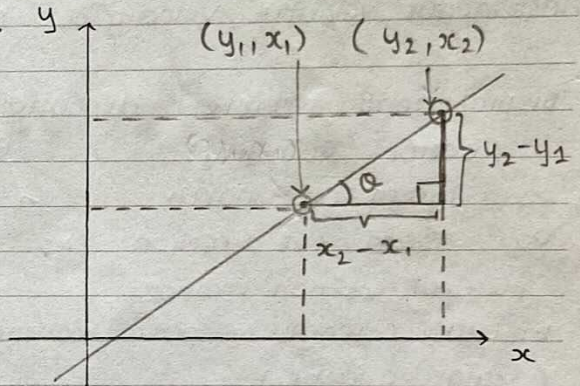
## Velocity time graph.

SLOPE → acceleration.

$$(v \div t)$$

AREA UNDER GRAPH / LINE → displacement

$$(v \times t)$$



$$\tan \theta = \frac{y_2 - y_1}{x_2 - x_1} = \frac{y_1 - y_2}{x_1 - x_2}$$

$\tan \theta = \text{slope}$

## Acceleration time graph

SLOPE → x (nothing)

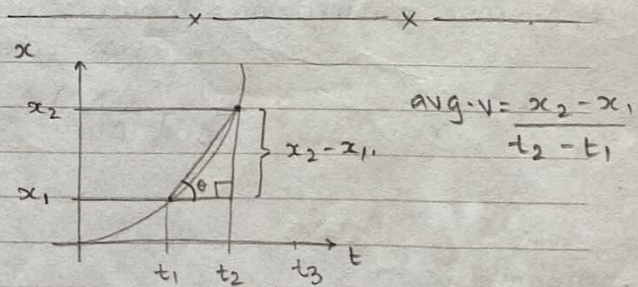
AREA UNDER GRAPH → Δ velocity. (a x t)

## Displacement time graph

SLOPE → velocity

## DISTANCE - TIME graph

SLOPE → speed.

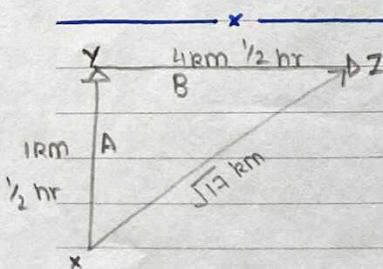


$$\text{avg. } v = \frac{x_2 - x_1}{t_2 - t_1}$$

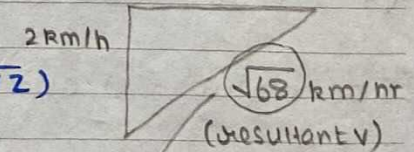
## Speed time graph

SLOPE → acceleration

AREA UNDER GRAPH → distance.



- A and B are displacement vectors
- From x to y ( $\vec{xy}$ ), From y to z ( $\vec{yz}$ )
- Overall disp =  $\vec{xz}$
- velocity  $\frac{y}{x} = \frac{1}{0.5} \text{ km/hr} = 2 \text{ km/hr}$



Different answers

★ Avg. velocity:  $\frac{\text{Disp}}{\text{total time}}$

$$\text{velocity } \frac{y}{z} = \frac{4}{0.5} \text{ km/hr} = 8 \text{ km/hr}$$

Total time taken to cover the distance. No Pythagoras for the time.

• Avg. velocity =  $\frac{\text{Disp}}{\text{TOTAL time}} = \frac{\sqrt{17}}{1/2 + 1/2} = \sqrt{17} \text{ km/hr}$

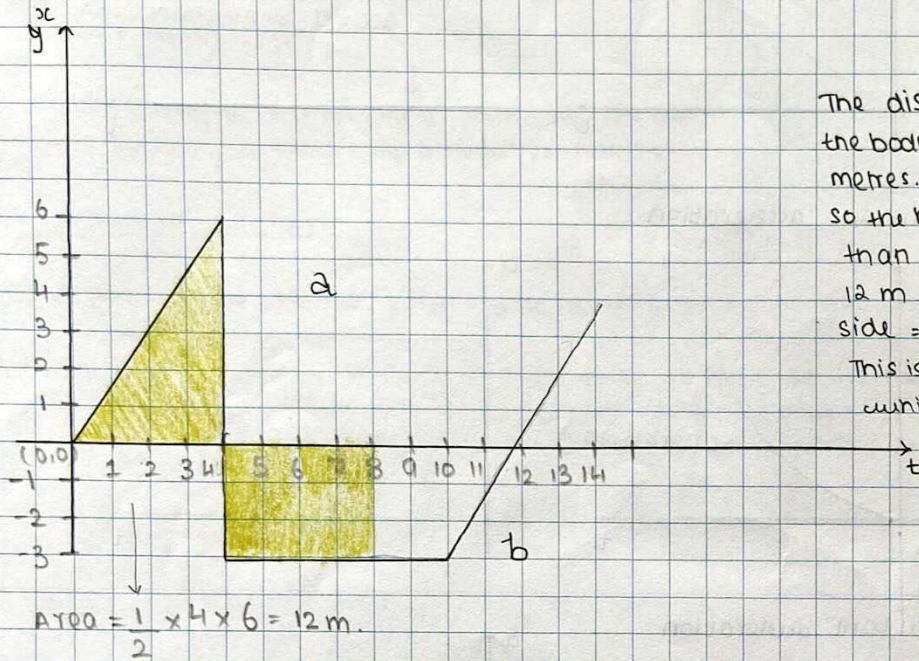


# GRAPHS

## Solving problems

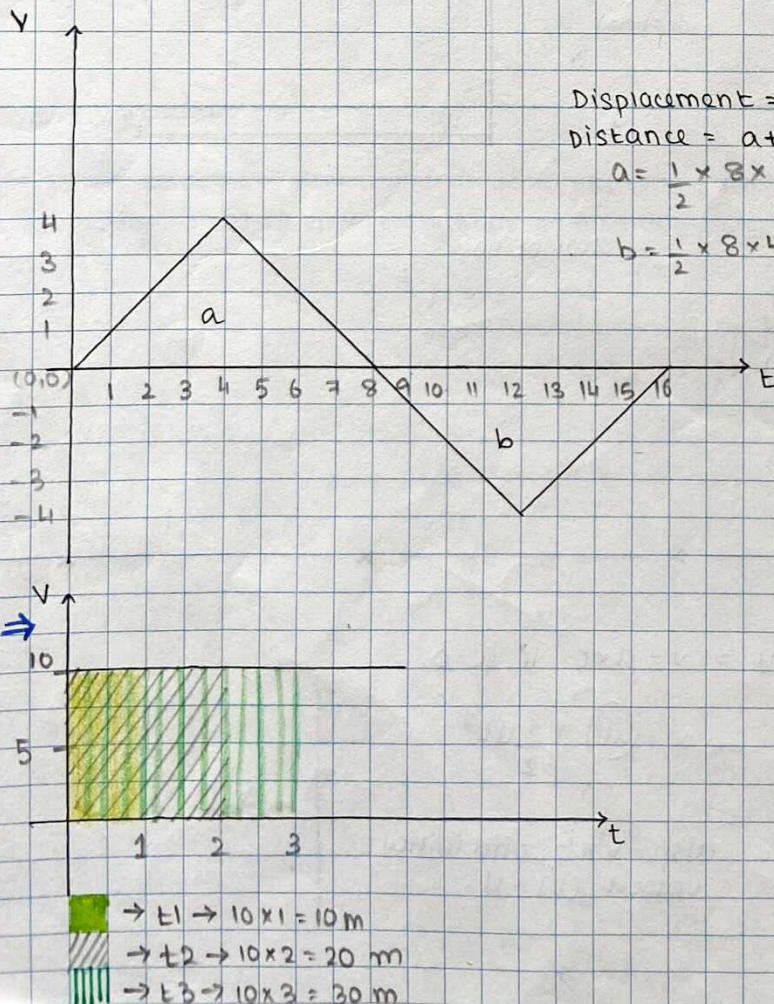
① If the body is at  $x=0$  and at  $t=0$ , when will it return to origin?

↓  
Find out when the displacement is cancelled out.



The displacement at  $a$  is positive  $\rightarrow$  so the body is moving to the right - and is 12 metres. The displacement at  $b$  is negative  $\rightarrow$  so the body moves to the left <sup>(towards its origin)</sup> - and is more than 12 m. when the displacement  $b$  reaches 12 m, the positive side = 12 m and negative side = -12 m so it cancels out. This is when the body is at 0 m  $(12 + (-12)) = 0$  which is its origin. this is at  $t = 8$  seconds.

② Find the distance and the displacement.



negative and positive velocity means the direction the body is travelling in.

↓  
negative velocity = reversed direction (left)  
 positive velocity = forward direction (right)  
 in some case positive v is taken as left

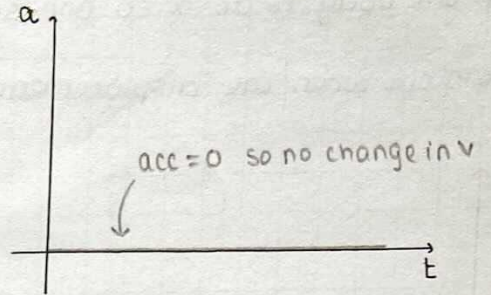
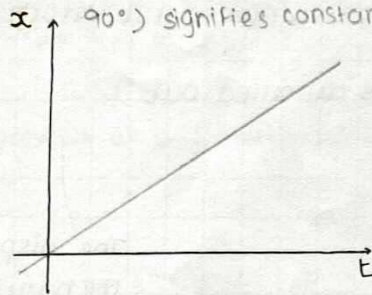
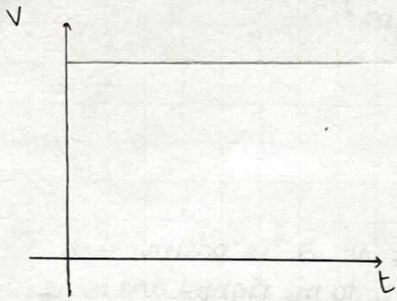
In the negative quadrant the '-' sign doesn't mean a literal -ve velocity! so -10 m/s means 10 m/s in the reversed direction / opposite direction.



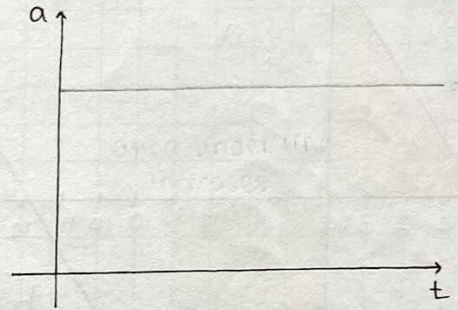
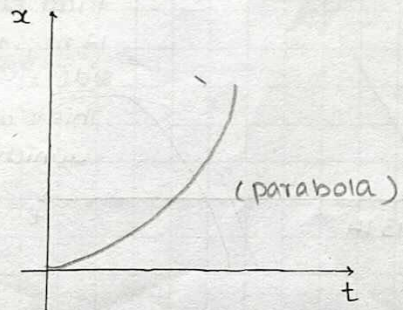
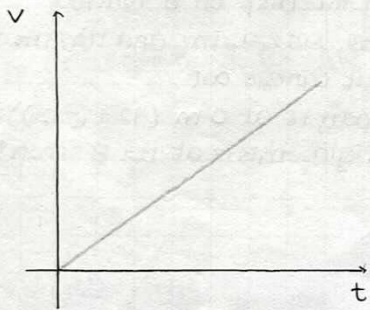
CASES.

CASE (i) constant velocity

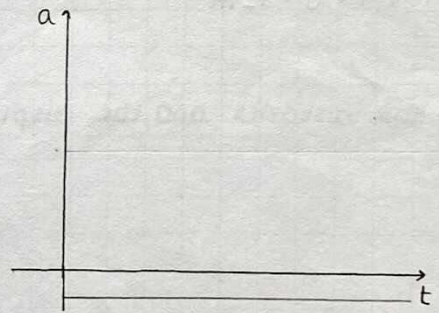
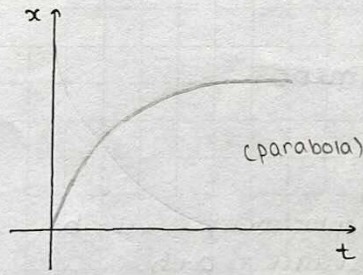
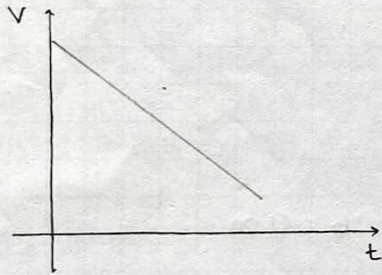
a straight line making any angle with the x axis (except  $90^\circ$ ) signifies constant  $v$



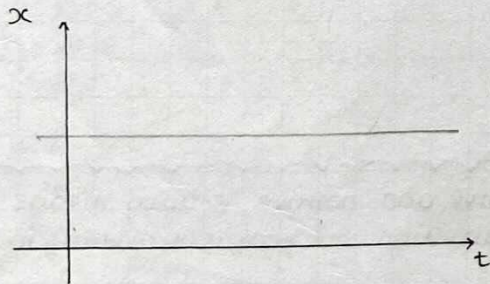
CASE (ii) increasing velocity, constant acceleration



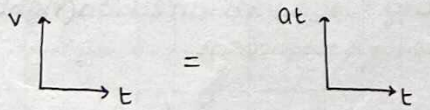
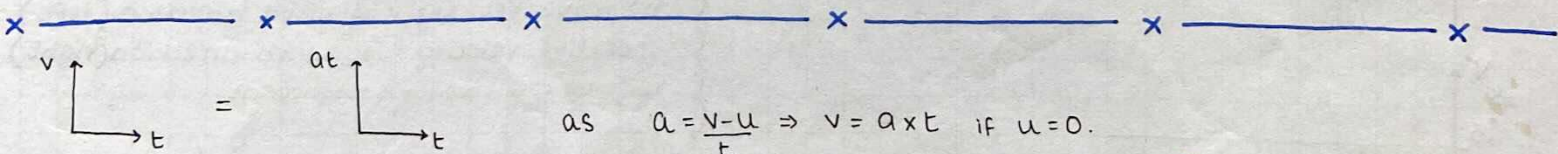
CASE (iii) Decreasing velocity, constant acceleration



CASE (iv) VELOCITY = 0.



(stationary object.)



as  $a = \frac{v-u}{t} \Rightarrow v = a \times t$  if  $u = 0$ .

disp =  $\frac{1}{2} \times b \times h$  :  $b = t$   $h = v = at$ .  
 $x = \frac{1}{2} \times t \times at = \frac{1}{2} at^2$

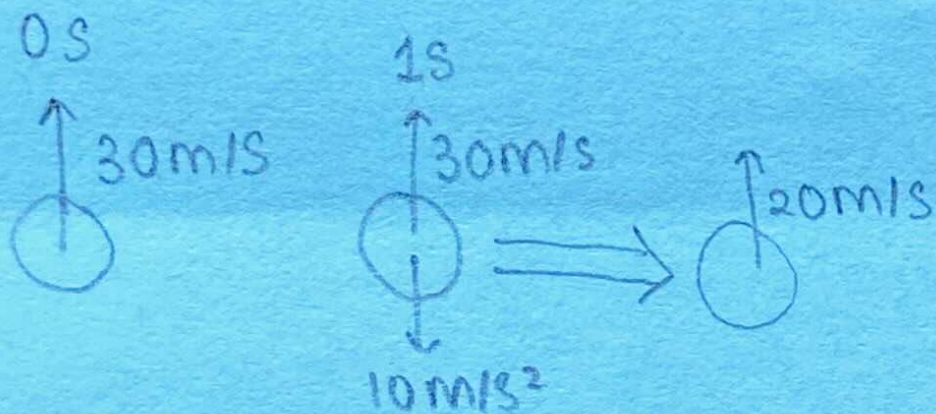
u = 0

$x = ut + \frac{1}{2}at^2$   
 disp =  $v \times t$ , and initial velocity (v) = u.

u  $\neq$  0



2.04



• Direction of acceleration = same direction as the net force.

•  $a =$  downwards here as the net force =  $mg =$  weight which acts downwards  
( $mg$  :  $m$  is scalar,  $g$  is  $\downarrow$ )

• (Balanced Forces :  $F_{\text{net}} = 0$  :  $a = 0$ )

•  $a = \frac{F}{m} = \frac{-mg}{m} = -g = -10\text{ m/s}^2$

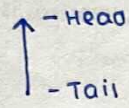
$$30\text{ m/s} + (-10\text{ m/s}) = 20\text{ m/s}$$

taking downward velocity as -ve.



# MORE ABOUT VECTORS

## Addition of vectors

- Representation of a vector quantity: 
- To add 2 vectors you have to know the direction and magnitude.

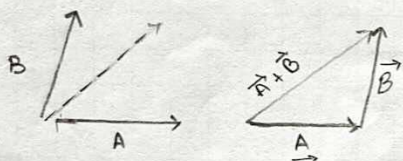
vector  $\times$  vector = vector  
vector  $\times$  scalar = vector

If we multiply a number by a positive no. the direction of the resulting vector remains the same.  
If we multiply a vector by a negative number the direction is reversed.

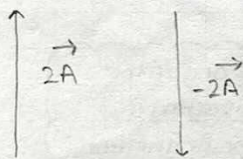
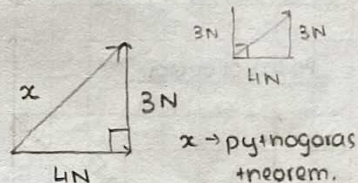
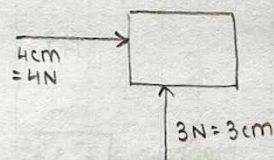
## Addition of 2 vectors

A vector can be shifted parallelly to itself (keeping length unchanged and direction unchanged)

Triangle law: shift vector ( $\vec{B}$ ) parallel to itself so its tail joins A's head.  
Join the remaining ends: resultant vector ( $\vec{A} + \vec{B}$ ). Its tail should join the free tail and head the free head.

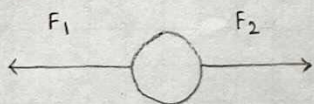


Eg:



## Force diagrams

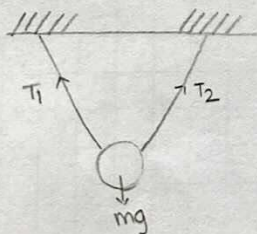
- A string develops a tension when a force acts on it. Tension in one string is unique to the string. The tension must be equal everywhere on the string.



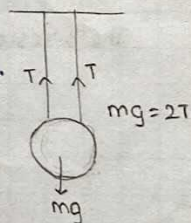
$$F_1 = F_2$$

when acceleration = 0, no change of uniform motion

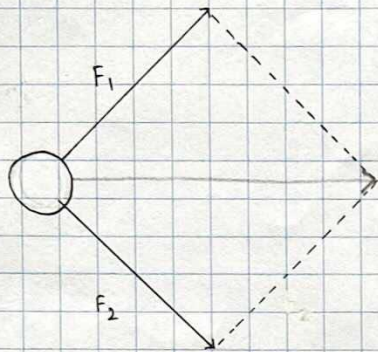
So  $F_{net} = 0$  and  $F_1 = F_2$  ( $F_1 + F_2 = 0$ ). ( $F_1 + F_2 = 0$ ; take one of the forces as -ve due to opp direction in this case)



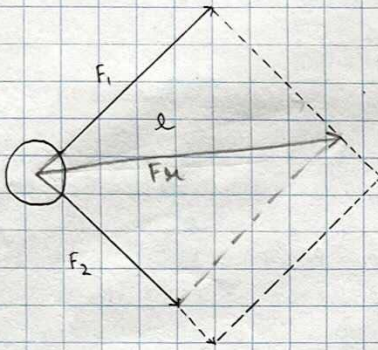
Symmetrical figure as strings' lengths are equal/same height.





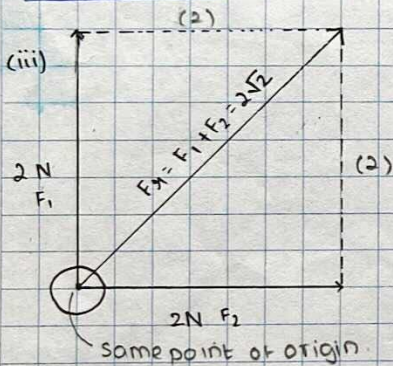


When you pull the strings with an equal force the ball moves diagonally so a quadrilateral is formed somewhere.  
 $F_1 = F_2$

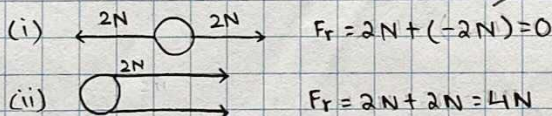


$F_R$  = resultant force.  
 $l$  → length of vector = magnitude of resultant.  
 • Parallelogram law of vector addition:  $\vec{F}_R = \vec{F}_1 + \vec{F}_2$   
 $F_1 > F_2$

Parallel vectors



Diagonal =  $\sqrt{2^2 + 2^2} = \sqrt{8} = \sqrt{4 \times 2} = 2\sqrt{2} \text{ N}$

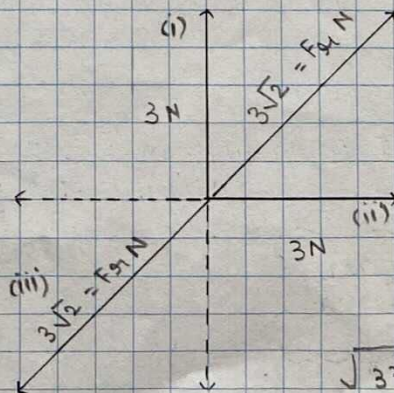
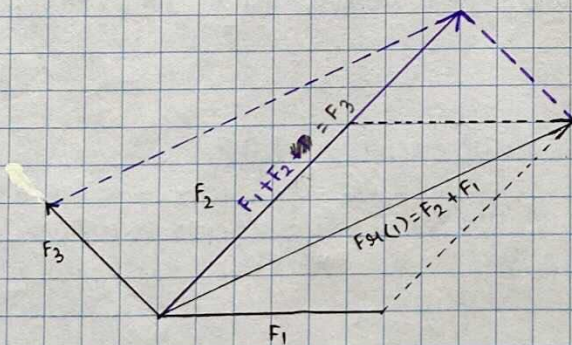


$F_r = 2\text{N} + (-2\text{N}) = 0$

$F_r = 2\text{N} + 2\text{N} = 4\text{N}$

-2N as one of the forces is acting in the opposite direction.

The 3 results of vector additions ( $\vec{2} + \vec{2}$ ) are (i) 0 (ii) 4N (iii)  $2\sqrt{2} \text{ N}$ , so:  $0 \leq \vec{2} + \vec{2} \leq 4$



It is possible for a number of concurrent forces to = 0. (concurrent forces act on the same point).

$\sum \vec{F}_i = 0$   $F_1 + F_2 + F_3 + \dots + F_n = 0$   
 (i = any no. of forces)

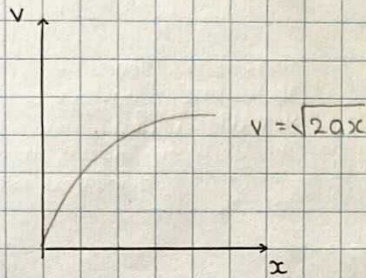
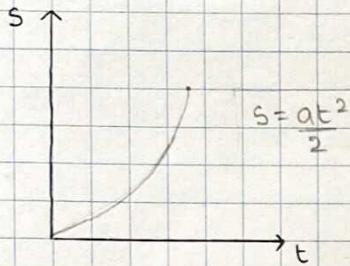
$\sqrt{3^2 + 3^2} = \sqrt{18} = \sqrt{9 \times 2}$   
 $= 3\sqrt{2} \text{ N}$



# MORE MOTION GRAPHS (PARABOLAS, CURVES)

## Parabolas.

$(y = ax^2 + bx + c)$



$v^2 = u^2 + 2ax$   
 $v^2 = 2ax$   $u=0$   
 $v = \sqrt{2ax}$

Displacement (s) is parabolic with respect to time for uniform accelerated motion.

uniform acceleration, so the graph is a parabola.

the equations such as  $s = \frac{at^2}{2}$  show that the  $\frac{at^2}{2}$  ratio increase is calculated through a formula and is not random. So, the equations show that the graph is a parabola

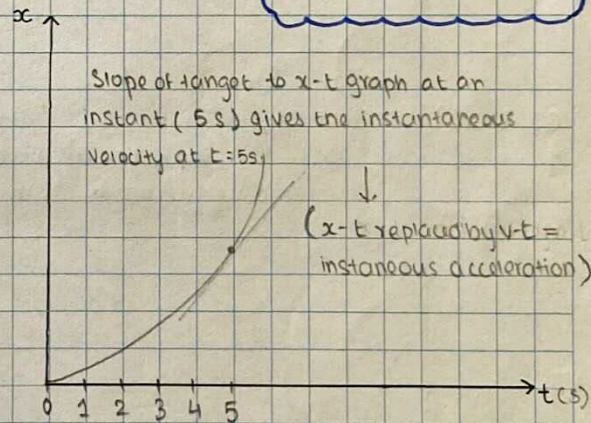
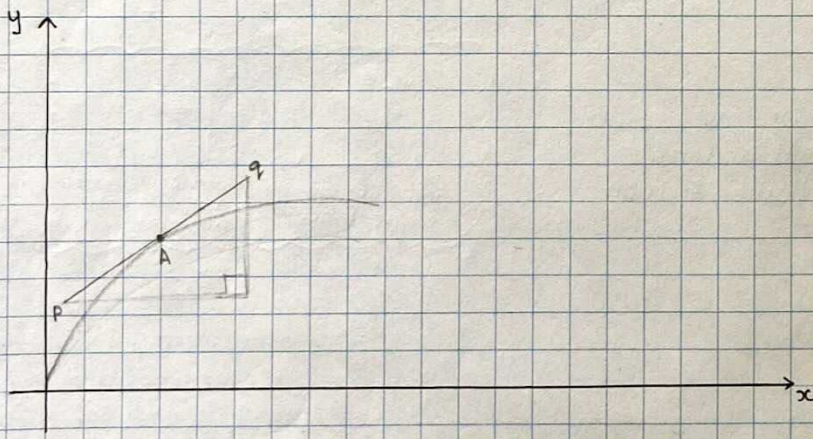
(A curve is a combination of infinity small, straight line segments (tangents) inclined at some angle)

### Slopes

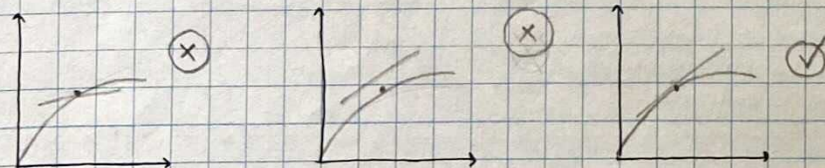
Specific point could be at a specific instant of time. eg at 2.5.

### (i) INSTANTANEOUS

The slope of a curve is found at a specific point by drawing a tangent. A tangent is a straight line touching the curve at that given point.



The slope of the tangent (p,q) gives the slope of the curve at that point.



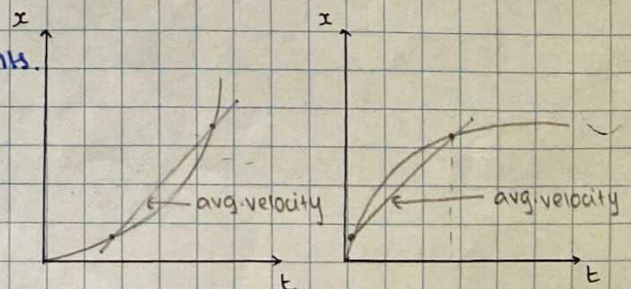
(X) = not a tangent  
 (✓) = tangent

### (ii) AVERAGE

Draw a secant.

A secant is a straight line that cuts a curve at two points.

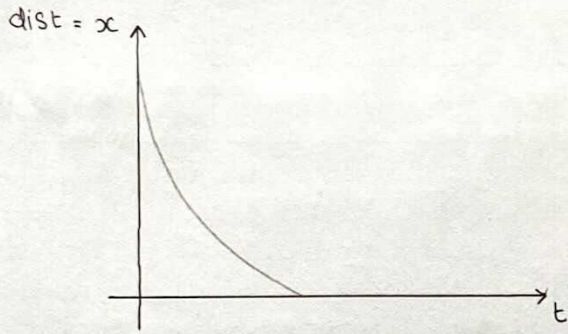
Slope of secant to x-t graph between 2 instants gives the average velocity between the 2 instants.





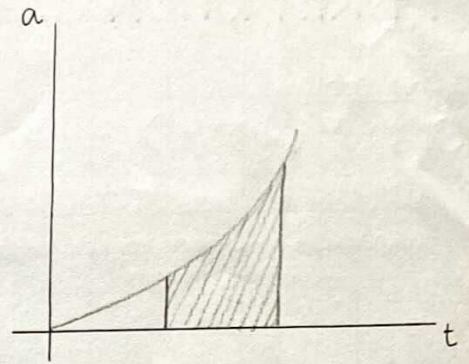
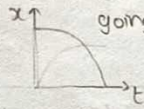
Cases

case (i) Decreasing speed



- Decreasing velocity as well

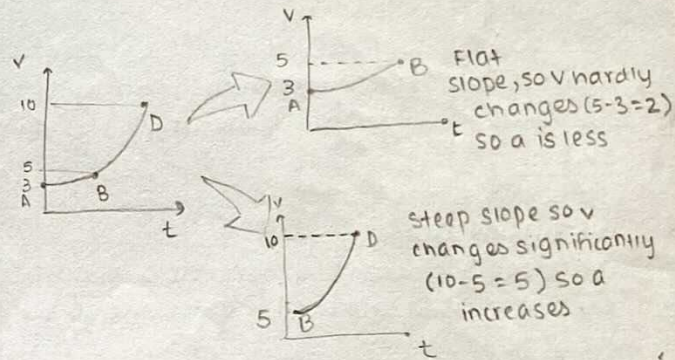
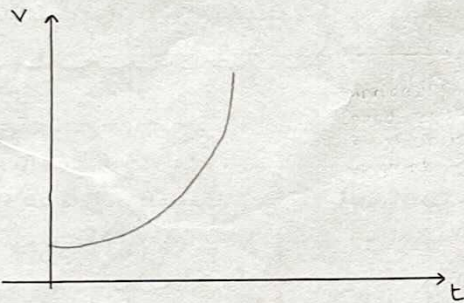
Increasing speed or increasing magnitude of velocity. However the velocity's direction is decreasing (going back to origin)



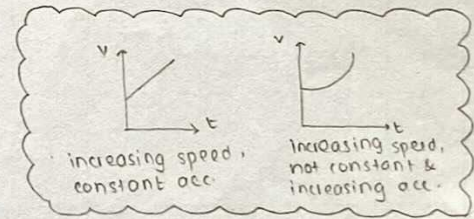
$$a = \frac{(v_2 - v_1)}{(t_2 - t_1)}$$

$$a(t_2 - t_1) = \Delta v$$

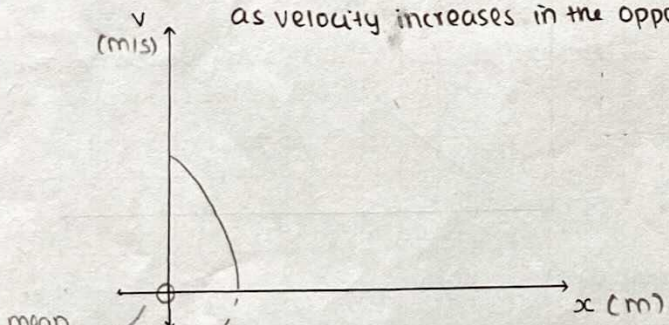
case (ii) Increasing acceleration



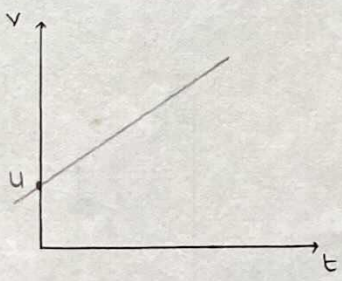
case (iii) Increasing displacement with reducing velocity and then the opposite displacement decreases as velocity increases in the opposite direction.



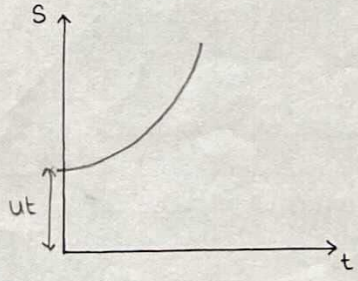
Eg: throwing up a ball  
eg: a pendulum: its velocity is max at mean position. The x signifies its amplitude, which increases as the velocity decreases at the extreme positions.



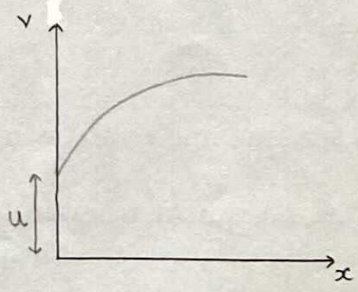
mean position (0,0)  
-4  
the velocity is -ve, but become '4' from '1'. The -ve simply means in the opposite direction, so the -ve sign can be removed and we get an increase in velocity from 1 to 4. m/s



$$v = u + at$$



$$s = ut + \frac{1}{2}at^2$$



$$v^2 = u^2 + 2as$$



Force  
Any kind of change that tends to bring about a change in state (state of rest / motion) or shape / size. Its presence is felt when it has an interaction with matter.

2.06

# FORCES IN BALANCE

Newton's 1st law of motion: law of inertia. (in a straightline)  
A body continues to be in its state of rest or uniform motion unless an external force is applied on it/ acted upon by an external, unbalanced force.

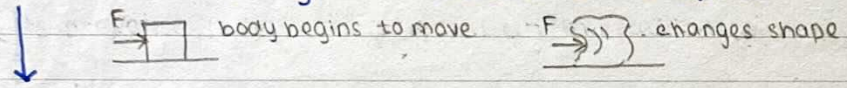
- Factors: (i) velocity (uniform motion in a straight line) remains constant.  
(ii) velocity changes only if  $\Sigma F \neq 0$ . net F (summation of F)  $\neq 0$

## Inertia

Resistance of any object to the application of force with respect to its change in state of motion / rest. In a physical object, mass is the inertia of any object.

## Force

- A physical / non-physical interaction that changes / tries to change the state of rest / motion in a straight line and/or the shape of an object.



- Assumption: no dissipation (loss) of energy.
- Any  $\Delta v$  implies the presence of an acceleration. So, a force brings about an acceleration.  $\Delta v = \text{Force involved}$ .  
 $\bar{F} \propto \bar{a}$  ( $\bar{a} \propto \bar{F}$ )

when energy transforms from 1 form to another, it tends to lose some energy in the form of heat energy, etc.

acc. is directly proportionate to the amt. of F applied.

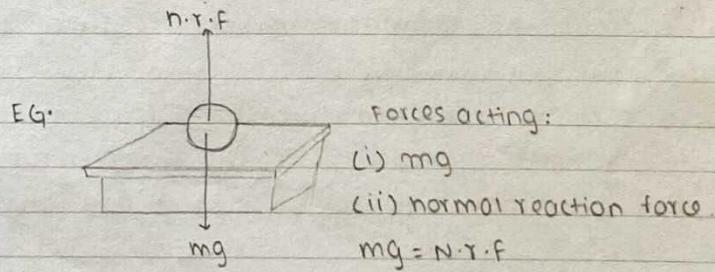
★ net force =  $m \times a$ .

## Forces in balance

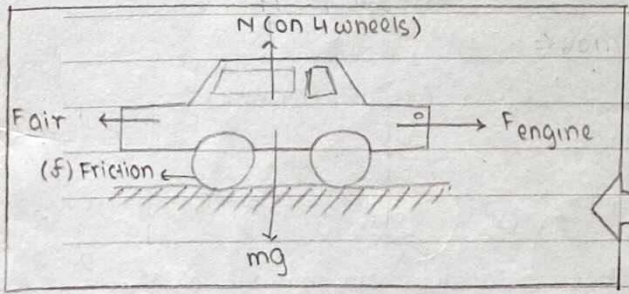
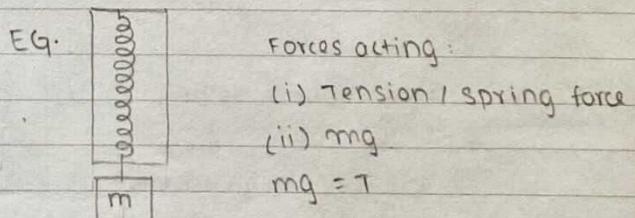
when the resultant force = 0.

Forces are in balance when:

- (i) either the body is at rest
- (ii) there is a constant velocity



support = normal reaction force.



Forces in vertical direction are balanced  $N = mg$   
Forces in horizontal direction are balanced  $F_{air} + f = F_{engine}$

( $F_{air}$  = air resistance)



# EFFECT OF AIR RESISTANCE

Air resistance  $\rightarrow F_{air}$

Net force  $\rightarrow F_{net}$

$F_{air}$   $\propto$  velocity / Speed.

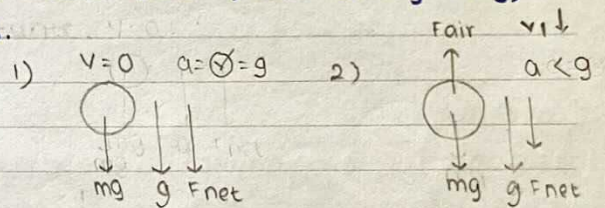
$F_{air}$   $\propto$  surface area.

Eq. 1) The moment a raindrop is dropped from the cloud:  $v = 0$ , force acting =  $mg$ ,

$F_{net}$ : downwards, acceleration: downwards.

$\downarrow$

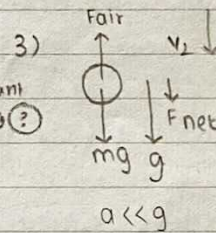
$F_{net}$  and  $a$  are the same magnitude.



2) As speed increases so does the air resistance.

$v = \text{present}$ ,  $F_{net} < g$

3) The speed further increases (due to  $a$ ) and the air resistance increases.  $F_{net} \ll g$ .

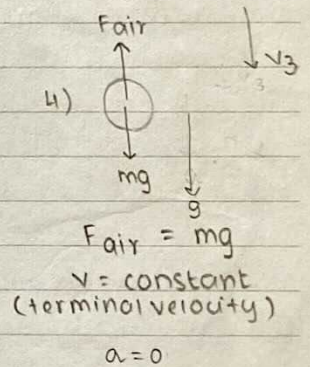


4) The forces are in balance,  $F_{net} = 0$ .

$\downarrow$

$F_{net} = m \times a$ , if  $a = 0$  (constant  $v$ ), then  $F_{net} = 0$ .

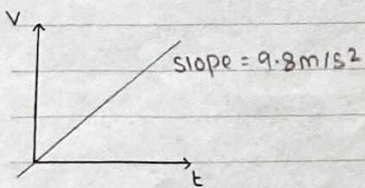
$a$  keeps reducing as  $a = \frac{F_{net}}{m}$  and  $F_{net}$  keeps decreasing.



## Acceleration is zero

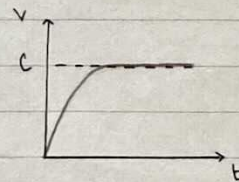
When someone jumps off a plane, their speed  $\uparrow$  so even  $F_{air} \uparrow$ , but there is the possibility that the terminal velocity is failed to reach and the person continues to accelerate. Even if terminal velocity is reached, it could be a  $v \uparrow$  terminal velocity you fall with: dangerous. The speed can't be controlled, but the surface area can. When the person opens his/her parachute the surface area is  $\uparrow$ , so the air resistance is  $\uparrow$ , helping the skydiver to reach their terminal velocity, and reach and land on the ground smoothly.

## Graphs

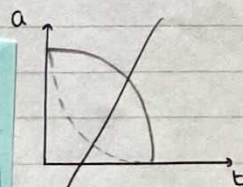
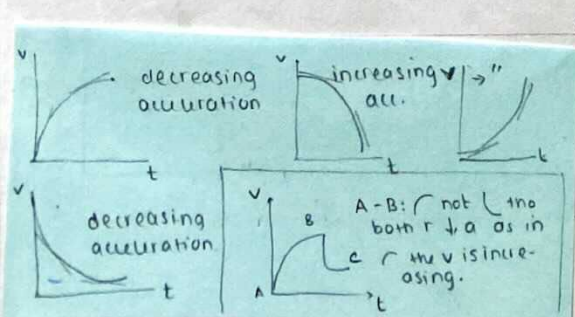


velocity of a falling body without  $F_{air}$ .

$$a = \frac{F}{m} = \frac{mg}{m} = g = 9.8 \text{ m/s}^2$$



velocity of a falling body with  $F_{air}$ .  
(Reaches terminal  $v$ )



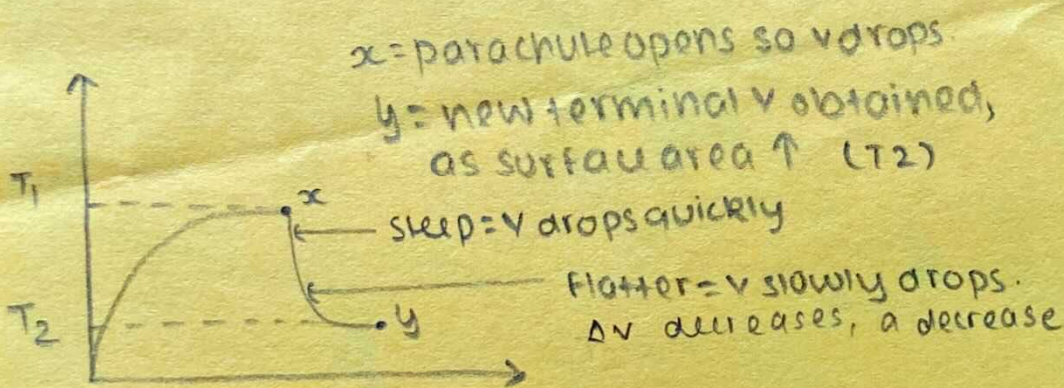
with  $F_{air}$  acc. changes at a slow rate initially as  $F_{air}$  is less due to the less speed.



$F_{net}$  decreases as the particle goes down. At a point  $F_{net} = 0$ , so  $a = 0$  and  $v = \text{constant}$ ; particle falls with constant  $v$  as the drag forces balanced the weight of the object.

Uniform / constant  $v = \text{terminal velocity}$

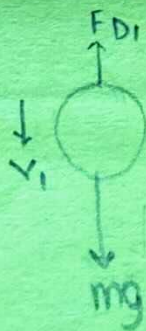
→ object moved in a fluid which offers some resistance to motion. Here, it is air resistance.



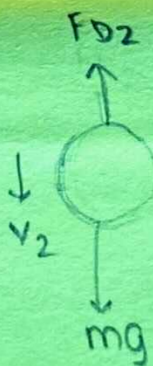
$v = 0 \quad F_D = 0$



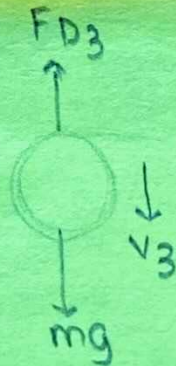
$F_{net} = mg$



$F_{net} = mg - F_{D1}$   
 $mg > F_{D1}$



$F_{net} = mg - F_{D2}$   
 $mg > F_{D2}$



$F_{net} = 0$   
 $mg = F_{D3}$

weight ( $mg$ ) balanced ←

• 1st case  $F_{net} = mg - F_D = mg - 0 = mg$ .  
 The net  $F$  is maximum.

• Last case  $F_{net} = mg - F_{D3}$  but they are equal, so  $F_{net} = 0$ .  $a = 0$   
 $v = \text{constant} = \text{terminal } v$ .

$v_3 > v_2 > v_1 > v_0$

$F_{D3} > F_{D2} > F_{D1}$

$v \propto F_D$

( $F_D$ : drag force)



2.07

# FORCE, MASS, ACCELERATION

$$\text{Resultant } F = \frac{mv - mu}{t} = m \frac{(v - u)}{t} = ma$$

Newton's 2nd law of motion:  $F = ma$ .  $F_{\text{net}} = ma$  directly

(The resultant force acting on a body is proportional to rate of change of momentum of the object. This change takes place in the direction of the resultant/applied force)

The acceleration of an object produced by net force = (i) directly proportional to the magnitude of the net force, (ii) same direction as the net force (iii) inversely proportional to the object's mass.

$$\bar{p} = m\bar{v}$$

Force to stop smthg  $\propto$  to mass and velocity.

Force  $\propto$  rate of change of momentum.

↓

$$F \propto \frac{\Delta p}{\Delta t}, \quad F = k \left( \frac{\Delta p}{\Delta t} \right) \quad k=1.$$

$$F = \frac{\Delta p}{\Delta t} = \frac{p_f - p_i}{\Delta t} = \frac{mv_f - mu_i}{\Delta t} = m \frac{(v_f - u_i)}{\Delta t} = ma \quad F = ma$$

Outcome of force: change in (i) state of rest (ii) velocity

2.08 (A motion or A direction)

# FRICTION

F = applied force

f = friction force.

or tendency of motion

1. Friction opposes / tries to oppose relative motion between the surfaces in contact.

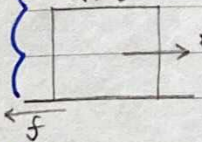
(and acts in a direction that does so  $\curvearrowright$ ). It is a surface phenomenon.

IT DOES NOT ALWAYS ACT IN THE OPPOSITE DIRECTION!

Friction is a force which acts at the contact of 2 surfaces. It acts equally on both surfaces (due to action x reaction).

If there is no motion  $F = f$ . When you apply a force but there is no motion, the object has a tendency to move but doesn't move.

$v=0$



$$\Sigma F = 0$$

Box: friction in the backward direction  $-x$  direction

Ground: Friction in the forward direction  $+x$  direction.

Relative motion  $\rightarrow$  way, friction  $\leftarrow$  way.

relative motion: one is fixed and the other is moving.

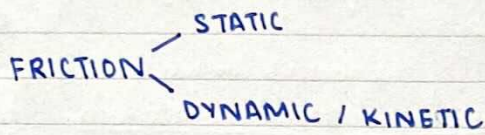
If friction is successful: no motion If failed: motion

Friction is a self-adjusting force when there is a tendency of motion but no actual motion

$\hookrightarrow$  static

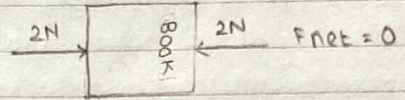
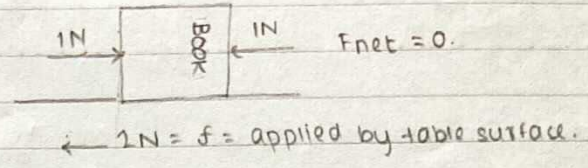
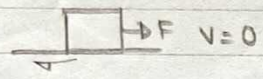


2. Friction is independent of area of contact.

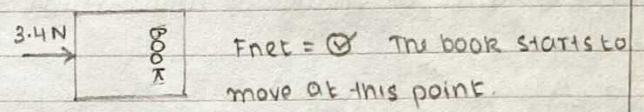


Static friction: friction acting between 2 surfaces when there is no relative motion between them / object is at rest.

(Friction is  $\uparrow$  so the object doesn't move.)

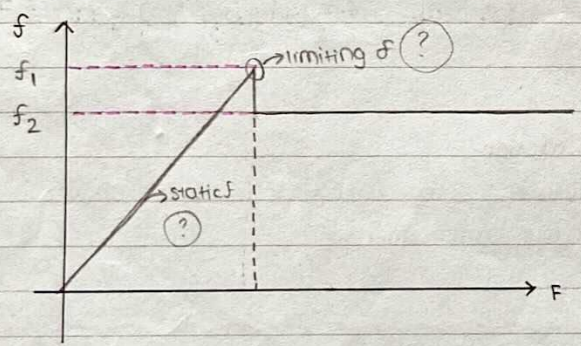
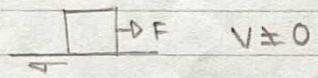


Friction increases, it adjusts its value so the net force = 0.



A jerk's yell, you can apply a little lower F to keep the object in motion (eg. 3.3 N).

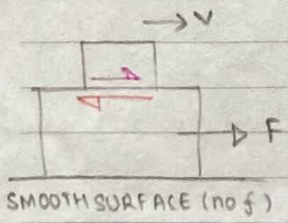
Dynamic friction: friction acting between 2 surfaces when there is a relative motion between them / when the object starts to move. Also called: kinetic friction



$f_1$  = limiting friction  
 $f_2$  = dynamic friction  
 throughout / the object is stationary.

to maintain a body's motion a F ( $F_1$ ) is required. when the body stops moving the surfaces interlock, the force ( $F_2$ ) required to remove this interlock is larger  $F_2 > F_1$

- when the F drops, F remains constant.
- when a body is in motion  $f =$  constant as long as the surface is the same. (dynamic friction remains unchanged)
- limiting friction: maximum frictional force. A surface can't infinitely apply / provide f. limiting friction > dynamic friction static f  $\xrightarrow{\text{limiting f}}$  dynamic F it is not static f.
- Factors for friction: (i) Nature of material (ii) Normal motion.



- both boxes move in  $\rightarrow$  direction, although there is no external F applied on the top box. The F that keeps it from falling (when the bodies are moving slowly the top box doesn't fall) is friction.
- If there was no f, the top box would fall ( $\downarrow \square \rightarrow$ ).
- The top box tries to remain at rest  $\rightarrow$  inertia.

applied by the big box on the small box  
 applied by small box on the big box



## FRICTION

Nature:  
wet/dry /  
rough/smooth

•  $f$  independent of :

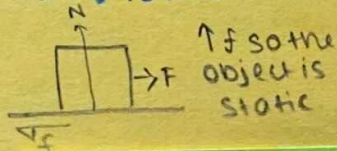
- (i)  $\bar{v}$ ,  $\bar{x}$ ,  $\bar{a}$
- (ii) area of contact

•  $f$  is dependant on:

- (i) Nature of surfaces in contact. (of material)
- (ii) Normal reaction.

Fundamental difference btwn static and dynamic  $f$ : static  $f$  is a self adjusting force while dynamic  $f$  is constant.

static  $f = F_{\text{applied}}$ , hence called a self-adjusting force.

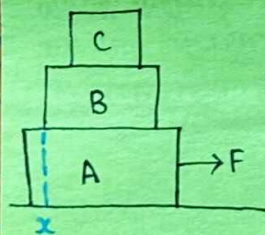


$$F = ma$$

↓  
Dissipative force is absent.  
Even if the force is very less, and the mass is very great there will be movement.

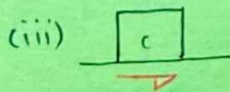
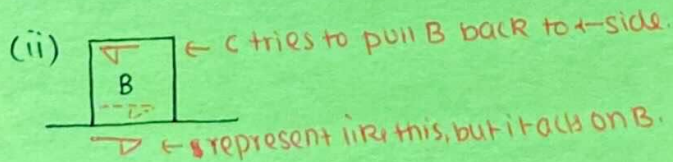
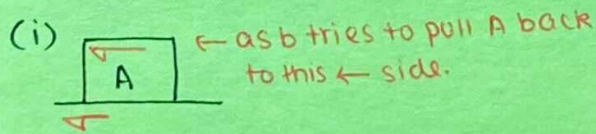
↓  
some amount of acceleration, according to the formula, will be possible.

static friction - amt. of applied force, so its called self adjusting force. It adjusts itself according to the  $F_s$  to match the  $F$



(Friction is present)

B's aim/tendency: to remain at the same point, x.





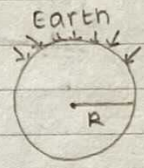
2.09

# FORCE, WEIGHT, AND GRAVITY

- $F = m \times a$ , but  $ma$  is not a force.
- $F = mg$   $a \Rightarrow g = \text{acceleration by Earth} = 9.8 \text{ m/s}^2$  (i) acc. due to gravity ( $9.8 \text{ m/s}^2$ ) (ii) gravitational field strength (10 N/Kg).  
 $g = \text{acceleration due to gravity.}$

we use 'g' as 'a' when the object is very close to the Earth's surface.

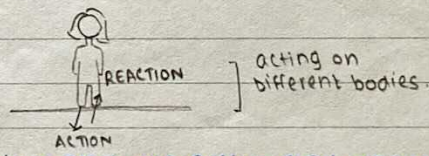
- if  $h \ll R$  then  $g = \text{constant}$   
 (h: height, R: Radius of Earth = 6400 Km,  $\ll$  = lesser than lesser than)



- $w = mg$ .  
 The weight of an object changes with  $g$ , so the weight of an object will be different on different planets. Mass never changes.  
 Eg: on moon:  $g$ 's value =  $1/6$  th of it on Earth.
- ↓  
 smaller the mass, smaller the gravitational pull (gravitational force, weight)

2.10

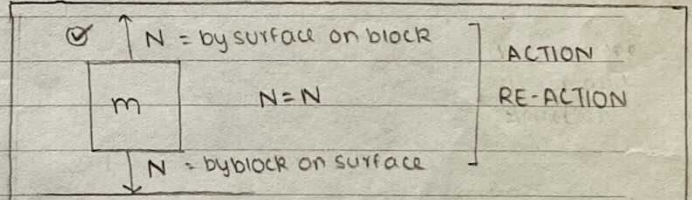
# ACTION AND RE-ACTION



Newton's 3rd law of motion:

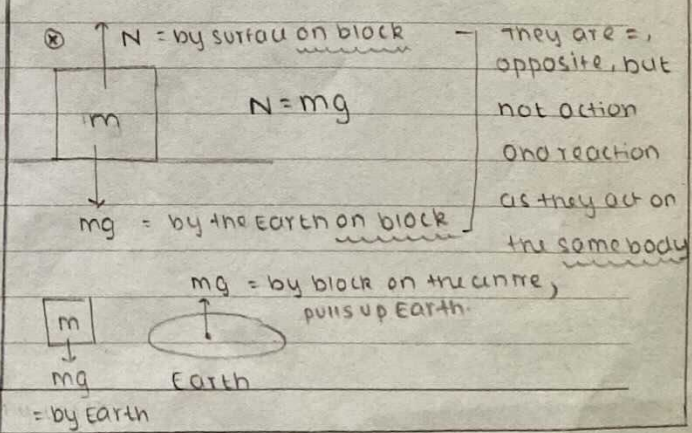
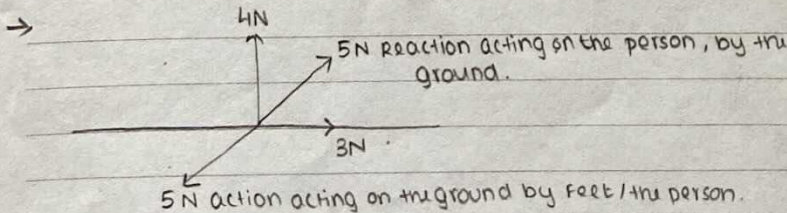
Every action has an equal but opposite re-action and the action and reaction forces act on 2 different objects.

When you press a wall, you feel a force on your arm. When the force you apply to press the wall increases, the force you feel in your arm also ↑.

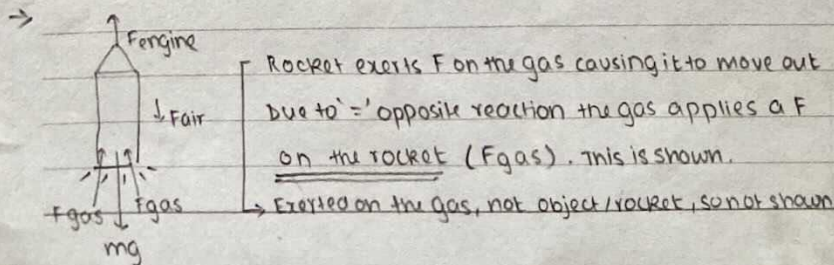


NOTE: The block (m) is actually on the table's surface, but has been separated/isolated to clarify the forces acting.

Eg. Walking  $\Rightarrow$  press a force backwards.



FREE BODY DIAGRAM (all Forces on object shown)

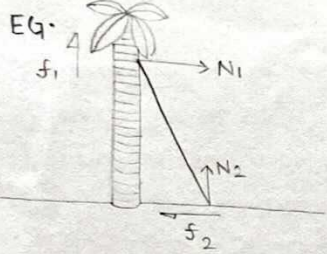




# Normal reaction

The force exerted by a surface on an object pressing against it.

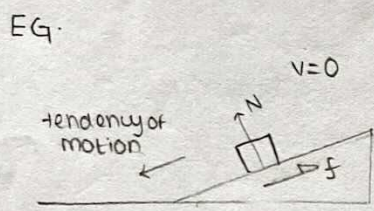
- Any  $F$  acting against a surface will create a reaction, that will act in a direction perpendicular to the surface and not on the direction of the applied force.



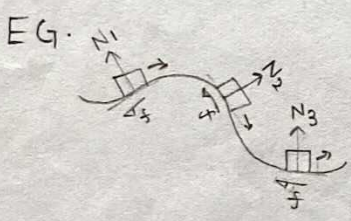
Ladder has  $F$  which it applies on the tree. The ladder tries to fall but the tree supports it. No tree then → falls

- $N_1$ : tree exerts on the ladder.
- $f_1$ : without this the ladder would fall DOWN so it must act UP.
- $f_2$ : ← direction as if there was motion of the ladder falling it would be in — direction.

- The normal reaction depends on the orientation of the surface: it is perpendicular to the surface.



the  $f$  keeps it from falling.



- Rough road →  $f$  present.
- for such a curved surface (i) draw a tangent. (ii) draw its perpendicular = Normal ( $N$ )



# FORCES IN BALANCE : NOTES.

0th order change (No change) : Displacement,  $x$ .

1st order change : Velocity,  $v = \frac{\Delta x}{\Delta t}$  (rate of change of displacement)

2nd order change : acceleration,  $a = \frac{\Delta v}{\Delta t} = \frac{\Delta}{\Delta t} \left( \frac{\Delta x}{\Delta t} \right) = \frac{\Delta^2 x}{\Delta t^2}$  (rate of change of velocity)

3rd order change : Jerk,  $\frac{\Delta^3 x}{\Delta t^3}$  (rate of change of acceleration)

(i) External Force ( $F_e$ ) acting.  $F_e = ma$ .

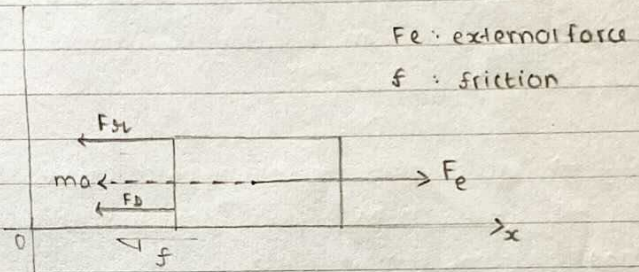
(ii) Friction is acting.  $F_e = ma + f$

(iii) Restoring force acting.  $F_e = ma + f + F_{st}$

(iv) Drag force  $F_e = ma + f + F_{st} + F_D$

↓

No other F acting beyond these 4.



$F_e$  : external force

$f$  : friction

(eliminating assumptions of  $F_D, F_r$ , etc. being absent)

Restoring force : restores the entire system back to its original form. It is present in springs and in pendulums (that is why the pendulum returns to its mean position).

brings object back to normal.

$F = kx$

Drag force : force felt by an object by the virtue of its motion in any viscous fluid.

$F_D \propto v$  acts in a direction opposite to  $v$ .

(If the object is in a fluid drag force is felt.)

(thick liquids feel a higher resistance to motion and have a greater viscosity).

$F_D = \beta v$  ( $\beta$  = constant, beta)

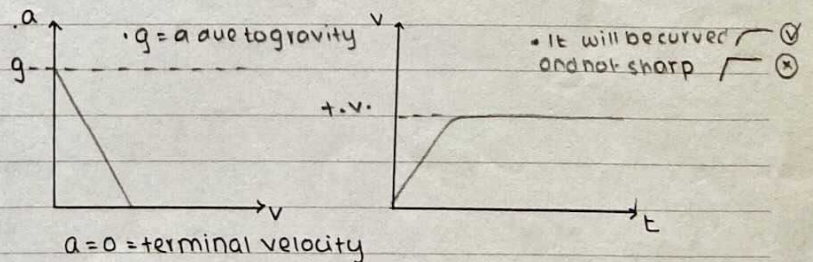
viscous : property of a fluid that resists motion of a solid thru it. Oil is more viscous than water. Not related to density, it is a separate property.

## FREE FALL

$F_e = m \times \frac{\Delta^2 x}{\Delta t^2} + f + kx + \beta \left( \frac{\Delta x}{\Delta t} \right)$

there is no  $f$  or  $kx$  during free fall.

$F_e = mg \rightarrow mg = \beta \left( \frac{\Delta x}{\Delta t} \right) + ma$   
 $ma = mg - \beta \left( \frac{\Delta x}{\Delta t} \right)$   
 $a = \frac{mg}{m} - \left[ \beta \left( \frac{\Delta x}{\Delta t} \right) \right] \div m$



(\*)  $a = g - \frac{\beta v}{m}$

↳  $\beta v$  = drag  $F \rightarrow a = g - \frac{F_{air}}{m}$

$a = g - \alpha v$  ( $\alpha$  = constant  $\alpha = \beta \div m$ )

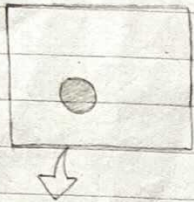
Friction : solid-solid surface  
 Drag force : solid-liquid surface.

(i) case : air resistance not taken  $\rightarrow \alpha = 0$ .  $a = g$

(ii) if  $v = 0$   $a = g$  (using the same formula)



# NOTES



This is the field:  $\square$

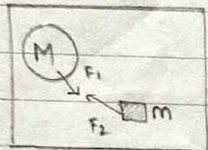
This is the mass:  $\circ$

The mass brings about a change in the field.

Mass  $\rightarrow \Delta$  gravitational field.

charge  $\rightarrow \Delta$  electric field

Magnet  $\rightarrow \Delta$  magnetic field.



M: huge mass  $\rightarrow$  eg. a galaxy/planet

m: regular object's mass

- (i)  $F_2 \rightarrow$  force of attraction acting on m applied by M. It pulls m towards M in  $\uparrow$  direction.
  - (ii)  $F_1 \rightarrow$  acting on M applied by m. It is the equal & opposite reaction for  $F_2$  acting on M.
- $F_1$  and  $F_2$  are not contact forces.

$F \propto \frac{1}{r^2}$  more the distance (further apart the objects) = weaker the force of attraction

$F \propto Mm$  More the masses = stronger the force of attraction.

$$F_g \propto \frac{Mm}{r^2}$$

$$F_g = G \frac{Mm}{r^2} \quad [G = \text{universal g.c. (gravitational constant)}]$$



2.11 and 2.12

# MOMENTUM(1) and (2)

$$\bar{p} = m\bar{v}$$

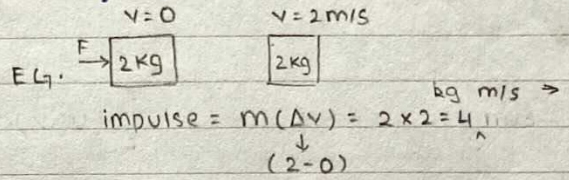
- p required = amt. of force required to stop a moving object.

(J)

$$\text{Impulse} = \text{change in momentum} = \Delta\bar{p}$$

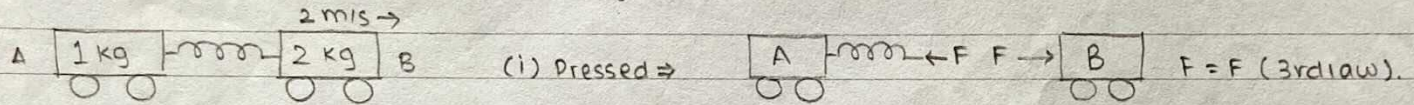
$$\Delta p = mv - mu = F \times t = F \times \Delta t$$

$$F = \frac{mv - mu}{t} = \frac{\Delta p}{\Delta t} = \bar{J} \quad F \Delta t = m \Delta v \text{ if } m = \text{constant}$$



- conservation principles  $\rightarrow$  momentum of a system is always conserved before and after a collision, provided no external forces are acting.

EG: 2 carts, A and B, are pressed against each other and released



F is a contact force (acts only when A and B are in contact)  $\rightarrow$  the time of contact between A and B will remain the same for A and for B; F is the same for A and B.

(Impulse =  $F \times t$  and  $= \Delta\bar{p}$ , so impulse for A and B remains the same).

(final  $\bar{p}$  - initial  $\bar{p}$ )

$$\Delta\bar{p} = (2 \times 2) - (2 \times 0) = 4 \text{ Ns.}$$

$$4 = m_A v_A - m_A \times 0 \Rightarrow v_A \times 1 = 4 \Rightarrow v_A = 4 \text{ m/s}$$

$$\bar{p} \text{ before release} = \bar{p} \text{ after release} \rightarrow (1 \times 0) + (2 \times 0) = (2 \times 2) + (1 \times v) \Rightarrow v = 0 - 4 = -4 \text{ m/s}$$

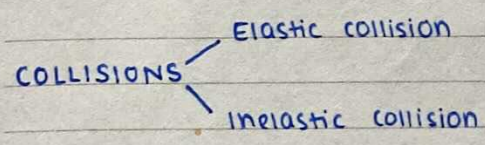
-4 m/s = opposite direction

NOTE the individual momentum for A and B will change, and there will be a net force on A & B.

But taking A and B together as a system,  $F_{\text{net}}$  acting on the system = 0.

$$F_{\text{net}} = \frac{\Delta\bar{p}}{t} \Rightarrow \Delta\bar{p} = 0 \times t = 0.$$

momentum before release = momentum after release. Thus, when a  $F_{\text{net}}$  acting on a system = 0, the total momentum of the system remains conserved.



## 1. Elastic collision

The K.E of the system remains conserved, K.E before collision = K.E after collision.

$$\frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2 = \frac{1}{2} m_1 v_1'^2 + \frac{1}{2} m_2 v_2'^2$$

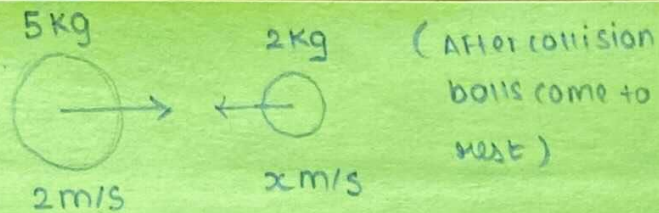
K.E =  $\frac{1}{2} m v^2$  formula.  
 $v' = v$  after collision

Total  $\bar{p}$  remains conserved

$$m_1 v_1 + m_2 v_2 = m_1 v + m_2 v = (m_1 + m_2) v$$

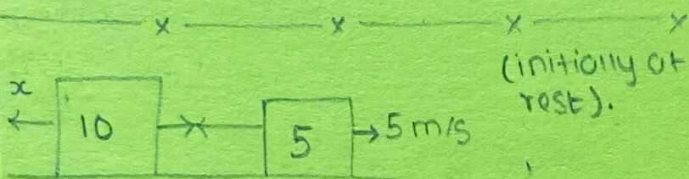
$$v = \frac{m_1 v_1 + m_2 v_2}{m_1 + m_2}$$





$$2x + 10 = 0 \quad x = -5 \text{ m/s}$$

(= 0 as final  $\vec{p} = 0$  as final  $\vec{v} = 0$ )



initial  $\vec{p} = 0 + 0 = 0$       initial  $\vec{p} = \text{final } \vec{p}$   
 Final  $\vec{p} = 25 + 10x$        $25 + 10x = 0 \quad x = -2.5 \text{ m/s}$

under the assumptions:

(i)  $a = \text{uniform}$

(ii) constant mass

$$\vec{F} = m\vec{a}$$

$F$  is rate of change of momentum.

If assumption isn't true,  $F = m \times \frac{\Delta v}{\Delta t}$

$$F = \frac{\Delta(mv)}{\Delta t}$$

change of  $x = \Delta x$

$$\text{Rate of change of } x = \frac{\Delta x}{t}$$

when there is an external force acting on the system the law of conservation of momentum doesn't apply.



law = momentum of a system is always conserved before and after a collision,

$$\text{Final } \vec{p} = \text{initial } \vec{p}$$

Q1) a ball mass 500g is travelling with a velocity of 72 kmph; the ball is brought to a rest in 0.4 s.

calculate avg. force.

Method # 1:      When writing avg. force the (—) sign isn't required.

$$72 \text{ kmph} = 20 \text{ m/s}$$

$$a = \frac{\Delta v}{t} = \frac{-20}{0.4} = -50 \text{ m/s}^2$$

$$F = ma = 0.5 \times -50 = -25 \text{ N}$$

Method # 2:

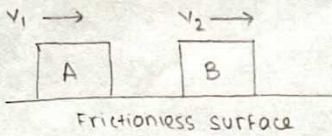
$$m = 0.5 \text{ kg} \quad u = 72 \text{ kmph} \quad v = 0$$

$$\Delta p = mv - mu \rightarrow F \cdot \text{avg} = \frac{\Delta p}{\Delta t} = \frac{m(v-u)}{t}$$

$$= 0.5(-20)/0.4 = -25 \text{ N}$$

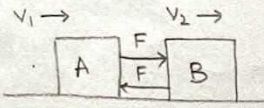


EG. ① BEFORE COLLISION



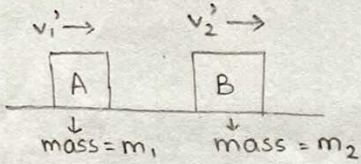
condition for them to collide  $\rightarrow v_1 > v_2$

② DURING COLLISION



Forces are equal and opposite, so momentum of the AB system remains conserved.

③ AFTER COLLISION



$v_2' > v_1'$  (changed v and changed greatness)

$$m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2'$$

- $\bar{p}$  before collision =  $\bar{p}$  after collision
- $F_{net}$  of system = 0

②

force acts in the opposite direction to velocity, so the velocity decreases.

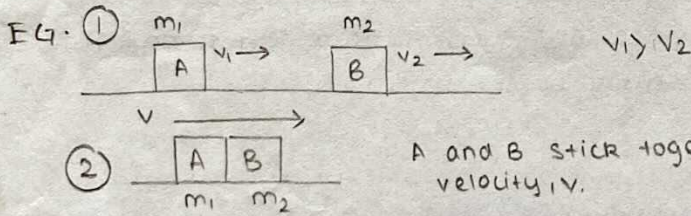
force's direction = velocity's direction, so velocity increases. The acceleration will be in the v's direction.

A and B move apart as B's v increases so much they move away.

2. inelastic collision

- Loss in K.E  $\rightarrow (\frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2) - \frac{1}{2} (m_1 + m_2) v^2 = \text{loss}$ .
- Momentum before = momentum after.

Some of the K.E is converted to P.E, you can't get the P.E back.



A and B stick together and move with the same velocity, v.

Inelastic : deforms permanently (energy lost)  
 Elastic : doesn't deform OR deforms and reforms (no energy lost)  
 ↓  
 eg. of partially elastic is dropping a rubber ball.

• momentum : answer, either write x kg m/s right or -x kg m/s (towards right).

•  $x > y$  Total  $\bar{p}$  after: A & B stick tog and move =  $x - y$  in  $\rightarrow$  direction (RIGHT)

$A \bar{p} = x$      $B \bar{p} = y$

$m_1 v_1 + m_2 v_2 = v(m_1 + m_2)$   
 $(8 \times 5) + (2 \times -5) = 10v$  momentum's direction  
 $v = 30 \div 10 = 3 \text{ m/s} \rightarrow$

•  $A = 8 \text{ kg } 5 \text{ m/s} \rightarrow$   
 $B = 2 \text{ kg } 5 \text{ m/s} \leftarrow$

collide, stick tog, move with v    total mass after collision =  $8 + 2 = 10 \text{ kg}$

$\bar{p} = (8 \times 5) - (5 \times 2) = 30 \text{ kg m/s} \rightarrow \bar{p} = m\bar{v} \rightarrow 30 = 10\bar{v} \rightarrow \bar{v} = \frac{30}{10} = 3 \text{ m/s} \rightarrow$